

Binomial Expansion

$$\begin{aligned}(X + 1)^1 &= X + 1 \\(X + 1)^2 &= 1X^2 + 2X + 1 \\(X + 1)^3 &= 1X^3 + 3X^2 + 3X + 1 \\(X + 1)^4 &= 1X^4 + 4X^3 + 6X^2 + 4X + 1 \\(X + 1)^5 &= 1X^5 + 5X^4 + 10X^3 + 10X^2 + 5X + 1 \\(X + 1)^6 &= 1X^6 + 6X^5 + 15X^4 + 20X^3 + 15X^2 + 6X + 1\end{aligned}$$

We did all of the painful multiplication and gathering of like terms in order to show you a nice pattern.

1. What do you notice?

2. Without actually doing the work of expanding the binomial, can you write out what $(X + 1)^7$ would become?

3. What expression would get us this simplified product?

$$1X^9 + 9X^8 + 36X^7 + 84X^6 + 126X^5 + 126X^4 + 84X^3 + 36X^2 + 9X^1 + 1$$

4. Can you figure out what $(X + 1)^{10}$ would become if you did all of the multiplication and simplification?

5. Explain in words how you would get the next row of expansions.